## Stage 3 Resource for assessing strategies: Addition and Subtraction

## Rubric for identifying counting and addition/subtraction strategies

Observe students during activity, tally or tick in the strategy box as you see it being used.
Class name:
Observer:
Date:

| Counts on using ones | Bridging to the decade | Friends of and to ten | Using doubles |
| :---: | :---: | :---: | :---: |
| Student counts on by ones for numbers of any size (including two-digit numbers) will use fingers or draw fence posts | Students bridge to ten by breaking up the second number <br> e.g. $17+5 ; 17$ and 3 is 20 then add two more makes 22 | Students combine numbers that add to 10 <br> e.g. $4+7+8+6+3+1$; group 4 and 6, 7 and 3 first <br> This can include friends of 6 , 7,8 and 9 as well. | Students use known facts like doubles and near doubles <br> e.g. $5+6$; double 5 then add one more |
| Counting on | Counting back | Using number facts | Jump strategy |
| Students count on from the larger number to find the total of two numbers <br> e.g. $14+7$, "I started with 14 and then count on seven more" $\begin{aligned} & 14,15,16,17,18,19,20, \\ & 21 \end{aligned}$ | Students count back from a number to find the number remaining <br> e.g. 17 - $\qquad$ = 14 " 1 started with 17 then counted back $16,15,14$ and I got $3^{\prime \prime}$ | Students use related addition and subtraction number facts to at least 20 $\begin{array}{ll} \text { e.g. } & 15+3=18 ; \\ \text { so } & 18-15=3 \end{array}$ <br> these are called 'Turn <br> Around Facts' | Students place the first number on an empty number line and then counts forward or backwards firstly by tens and then by ones to perform a calculation |
| Split Strategy | Compensation strategy | Using patterns to extend number facts | Bridging the decades |
| Students separate the tens from the units and add or subtract each separately before combining to obtain the final answer $\text { e.g. } \begin{aligned} & 46+33 \\ & =40+6+30+3 \\ & =40+30+6+3 \\ & =70+9 \\ & =79 \end{aligned}$ | Students 'round up' a number that is close to the decade to make the calculation simpler. $\text { e.g. } 63+29 ; 63+30 \text { is } 93,$ subtract 1, to obtain 92 | Students see the similarity between calculations of smaller and larger numbers, using an easier sum as a starting place for finding a solution. $\begin{aligned} & \text { e.g. } 5-2=3 \text {, so } 500-200 \text { is } \\ & 300 \end{aligned}$ | This strategy is similar to using a split strategy, instead of splitting both numbers, students keep one number whole and bridge to the decade first. $\begin{aligned} & \text { e.g. } 34+26 ; 34+6=40,40+ \\ & \quad 20=60 \end{aligned}$ <br> It is a reversal of jump but is only used when the 'ones' add to a ten |
| Forming multiples | Formal algorithm | Partitioning numbers | Inverse operations |
| Student change the order of addends (numbers) to form multiples of ten or other decades. <br> e.g. $16+8+4$; add 16 and 4 first | Students use a formal algorithm to record their calculations. <br> e.g. $\begin{aligned} & 134+ \\ & 568 \end{aligned}$ | Students can expand numbers into standard and nonstandard forms to make addition or subtraction easier. $\begin{aligned} & \text { e.g. } 500+670: 670=500+ \\ & 170, \text { so } 500+670=500+500 \\ & \text { (or } 2 \times 500 \text { ) }=1000+170= \\ & 1170 \end{aligned}$ | Students check solutions by using inverse operations. $\text { e.g. } 50-27=23 \text {, so, } 23+27=$ $50$ |

Stage 3 Resource for assessing strategies: Multiplication and Division
Rubric for identifying multiplication and division strategies
Observe students during activity, tally or tick in the strategy box as you see it being used.
Class name:
Observer:
Date:

| Model equal groups | Perceptual counting and sharing | Rhythmic counting | Skip counting |
| :---: | :---: | :---: | :---: |
| 'two groups of three' | Uses visual markers to represent items and groups | $1,2,3,4,5,6,7,8,9 .$. | $3,6,9,12 \ldots$ <br> May need visible items |
| Forms arrays of equal rows | Figurative- multiple count | Uses repeated addition for multiplication | Uses repeated subtraction for division |
|  | Uses visual markers to represent groups $\begin{array}{\|ccc\|} \hline \begin{array}{\|c\|} \hline 5 \\ \hline \end{array} & \begin{array}{\|c\|} \hline 5 \\ 3 \end{array} & \begin{array}{\|c} 5 \\ \hline \end{array} \\ \hline \end{array}$ | 5 groups of 4 is the same as $4+4+4+4+4$ <br> Or <br> For $3 \times 4$ $3+3 \text { is } 6,6+3 \text { is } 9,9+3 \text { is } 12$ | $\begin{aligned} & 25 \div 5= \\ & 25-5=20 \text { (one) } \\ & -5=15 \text { (two) } \\ & -5=10 \text { (three) } \\ & -5=5 \text { (four) } \\ & -5=0 \text { (five) } \end{aligned}$ |
| Uses a double count to coordinate composite units | Uses doubling and repeated doubling | Uses halving and repeated halving for 2,4 and 8 | Uses inverse operations |
| Counts by the number in each group while counting the number of groups e.g. "How many three in 18 ?" 3 is 1,6 is 2,9 is $3 \ldots 18$ is 6 | $7 \times 8$ is double 7 (14), double again (28) then double again (56) | $36 \div 4$ :halve 36 (gives 18) then halve again (equals 9) | $25 \div 5$ is the same as $5 \times ?=25$ so the answer is 5 |
| Uses known facts to work out unknown | Uses relationships between facts | Uses place value concepts | Factorises the multiple of 10 |
| $5 \times 7=35$ so $6 \times 7$ is 7 more than 35 | Multiples for 6 are double the facts for 3 | $3 \times 20$ is the same as $3 \times 2$ tens $=6$ tens $=60$ | $3 \times 20$ is the same as $3 \times 2 \times 10=6 \times 10=60$ |
| Model commutative property | Multiplying the tens then the units | Model and apply associative property | Factorising the larger number |
| 3 groups of 2 is the same as 2 groups of 3 | $7 \times 19$ is the same as 7 tens plus 7 nines is $70+63=$ 133 | $2 \times 3 \times 5=2 \times 5 \times 3=10 \times 3=30$ | $18 \times 5=9 \times 2 \times 5=9 \times 10=90$ |
| Uses an area model | Uses a formal algorithm (Stage 3 M\&D 1) | Uses extended form (long multiplication) <br> (Stage 3 M\&D 1) | Uses estimation (Stage 3 M\&D 1) |
|  | $\begin{array}{r} 432 x \\ 5 \\ \hline 2160 \\ \hline \end{array}$ | $\begin{array}{r} 521 \mathrm{x} \\ 222 \\ \hline 10420 \\ \hline 11462 \\ \hline \end{array}$ | $32 \times 253$ will be about, but more than $30 \times 250$ |
| Recognises grouping symbols (Stage 3 M\&D 2) | Applies order of operations (Stage 3 M\&D 2) |  |  |
| $5+(2 \times 3)=5+6=11$ | $32 \div(2 \times 4)=32 \div 8=4$ <br> (grouping symbols first) |  |  |

